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Simulating melodic and harmonic expectations for tonal cadences using probabilistic models

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ABSTRACT
This study examines how the mind’s predictive mechanisms contribute to the perception of cadential closure during music listening. Using the Information Dynamics of Music model (or IDyOM) to simulate the formation of schematic expectations—a finite-context (or n-gram) model that predicts the next event in a musical stimulus by acquiring knowledge through unsupervised statistical learning of sequential structure—we predict the terminal melodic and harmonic events from 245 exemplars of the five most common cadence categories from the classical style. Our findings demonstrate that (1) terminal events from cadential contexts are more predictable than those from non-cadential contexts; (2) models of cadential strength advanced in contemporary cadence typologies reflect the formation of schematic expectations; and (3) a significant decrease in predictability follows the terminal note and chord events of the cadential formula.

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Cadence; expectation; statistical learning; segmental grouping; n-gram models

1. Introduction

In the intellectual climate now prevalent, many scholars view the brain as a ‘statistical sponge’ whose purpose is to predict the future (Clark, 2013). While descending a staircase, for example, even slightly misjudging the height or depth of each step could be fatal, so the brain predicts future steps by building a mental representation of the staircase, using incoming auditory, visual, haptic and proprioceptive cues to minimise potential prediction errors and update the representation in memory. Researchers sometimes call these representations schemata—‘active, developing patterns’ whose units are serially organised, not simply as individual members coming one after the other, but as a unitary mass (Bartlett, 1932, p. 201). Over the course of exposure, these schematic representations obtain greater specificity, thereby increasing our ability to navigate complex sensory environments and predict future outcomes.

Among music scholars, this view was first crystallised by Meyer (1956, 1967), with the resurgence of associationist theories in the cognitive sciences—which placed the brain’s predictive mechanisms at the forefront of contemporary research in music psychology—following soon thereafter. Krumhansl (1990) has suggested, for example, that composers often exploit the brain’s potential for prediction by organising events on the musical surface to reflect the kinds of statistical regularities that listeners will learn and remember. The tonal cadence is a case in point. As a recurrent temporal formula appearing at the ends of phrases, themes and larger sections in music of the common-practice period, the cadence provides perhaps the clearest instance of phrase-level schematic organisation in the tonal system. To be sure, cadential formulae flourished in eighteenth-century compositional practice by serving to ‘mark the breathing places in the music, establish the tonality, and render coherent the formal structure’, thereby cementing their position ‘throughout the entire period of common harmonic practice’ (Piston, 1962, p. 108). As a consequence, Sears (2015, 2016) has argued that cadences are learned and remembered as closing schemata, whereby the initial events of the cadence activate the corresponding schematic representation in memory, allowing listeners to form expectations for the most probable continuations in prospect. The subsequent realisation of those expectations then serves to close off both the cadence itself, and perhaps more importantly, the longer phrase-structural process that subsumes it.

There is a good deal of support for the role played by expectation and prediction in the perception of closure (Huron, 2006; Margulis, 2003; Meyer, 1956; Narmour, 1990), with scholars also sometimes suggesting that listeners possess schematic representations for cadences and other recurrent closing patterns (Eberlein, 1997; Eberlein & Fricke, 1992; Gjerdingen,
demonstrated the degree to which IDyOM can simulate the responses of listeners in tasks involving melodic segmentation (Pearce, Müllensiefen, & Wiggins, 2010), subjective ratings of predictive uncertainty (Hansen & Pearce, 2014), subjective and psychophysiological emotional responses to expectancy violations (Egermann, Pearce, Wiggins, & McAdams, 2013), and behavioural (Omigie, Pearce, & Stewart, 2012; Pearce & Wiggins, 2006; Pearce, Ruiz, Kapasi, Wiggins, & Bhattacharya, 2010), electrophysiological (Omigie, Pearce, Williamson, & Stewart, 2013), and neural measures of melodic pitch expectations (Pearce, Ruiz, et al., 2010). And yet, the majority of these studies were limited to the simulation of melodic pitch expectations, so this investigation develops new representation schemes that also permit the probabilistic modelling of harmonic sequences in complex polyphonic textures.

To consider how IDyOM might simulate schematic expectations in cadential contexts, this study adopts a corpus- analytic approach, using the many methods of statistical inference developed in the experimental sciences to examine a few hypotheses about cadential expectations. To that end, Section 2 provides a brief summary and discussion of the cadence concept, as well as the typology on which this study is based (Caplin, 1998, 2004), and then offers three hypotheses designed to examine the link between prediction and cadential closure. Next, Section 3 introduces the multiple viewpoints framework employed by IDyOM, and Section 4 describes the methods for estimating the conditional probability function for individual melodic or harmonic viewpoints using maximum likelihood (ML) estimation and the prediction-by-partial-match (PPM) algorithm. We then present in Section 5 the corpus of expositions and the annotated cadence collection from Haydn’s string quartets and describe Pearce’s procedure for improving model performance by combining viewpoint models into a single composite prediction for each melodic or harmonic event in the sequence. Finally, Section 6 presents the results of the computational experiments, and Section 7 concludes by discussing limitations of the modelling approach and considering avenues for future research.

2. The classical cadence

Like many of the concepts in circulation in music scholarship (e.g. tonality, harmony, phrase, meter), the cadence concept has been extremely resistant to definition. To sort through the profusion of terms associated with cadence, Blommbach (1987) surveyed definitions in eighty-one textbooks distributed around a median publication date of 1970. Her findings suggest that the cadence...
is most frequently characterised as a *time span*, which consists of a conventionalised harmonic progression, and in some instances, a ‘falling’ melody. In over half of the textbooks surveyed, these harmonic and melodic formulae are also classified into a compendium of cadence types, with the degree of finality associated with each type sometimes leading to comparisons with punctuation in language. However, many of these definitions also conceptualise the cadence as a ‘point of arrival’ (Ratner, 1980), or *time point*, which marks the conclusion of an ongoing phrase-structural process, and which is often characterised as a moment of rest, quiescence, relaxation or repose. Thus a cadence is simultaneously understood as time-span and time-point, the former relating to its most representative (or recurrent) features (cadence as *formula*), the latter to the presumed boundary it precedes and engenders (cadence as *ending*) (Caplin, 2004).

The compendium of cadences and other conventional closing patterns associated with the classical period is enormous, but contemporary scholars typically cite only a few, which may be classified according to two fundamental types: those cadences for which the goal of the progression is tonic harmony (e.g. perfect authentic, imperfect authentic, deceptive, etc.), and those cadences for which the goal of the progression is dominant harmony (e.g. half cadences). Table 1 provides the harmonic and melodic characteristics for five of the most common cadence categories from Caplin’s typology (1998, 2004).

<table>
<thead>
<tr>
<th>Types</th>
<th>Categories</th>
<th>Essential characteristics</th>
<th>N</th>
</tr>
</thead>
<tbody>
<tr>
<td>PAC</td>
<td>Perfect Authentic</td>
<td>V–I 1</td>
<td>122</td>
</tr>
<tr>
<td>IAC</td>
<td>Imperfect Authentic</td>
<td>V–I 3 or 5</td>
<td>9</td>
</tr>
<tr>
<td>DC</td>
<td>Deceptive (DC)*</td>
<td>V–?, Typically vi 1 or 3</td>
<td>19</td>
</tr>
<tr>
<td>EV</td>
<td>Evaded (EV)*</td>
<td>V–?, 7, Typically 5</td>
<td>11</td>
</tr>
<tr>
<td>HC</td>
<td>Half (HC)</td>
<td>?–V 5, 7, or 2</td>
<td>84</td>
</tr>
</tbody>
</table>

The perfect authentic cadence (PAC), which features a harmonic progression from a root-position dominant to a root-position tonic, as well as the arrival of the melody on 1, serves as the quintessential closing pattern not only for the high classical period (Gjerdingen, 2007), but for repertories spanning much of the history of Western music. The imperfect authentic cadence (IAC) is a melodic variant of the PAC category that replaces 1 with 3 (or, more rarely, 5) in the melody, and like the PAC category, typically appears at the conclusion of phrases, themes, or larger sections.

The next two categories represent cadential deviations, in that they initially promise a perfect authentic cadence, yet fundamentally deviate from the pattern’s terminal events, thus failing to achieve authentic cadential closure at the expected moment Caplin calls *cadential arrival* (1998, p. 43). The deceptive cadence (DC) leaves harmonic closure somewhat open by closing with a non-tonic harmony, usually vi, but the melodic line resolves to a stable scale degree like 1 or 3, thereby providing a provisional sense of ending for the ongoing thematic process. The evaded cadence is characterised by a sudden interruption in the projected resolution of the cadential process. For example, instead of resolving to 1, the melody often leaps up to some other scale degree like 5, thereby replacing the expected ending with material that clearly initiates the subsequent process. Thus, the evaded cadence projects no sense of ending whatsoever, as the events at the expected moment of cadential arrival, which should group backward by ending the preceding thematic process, instead group forward by initiating the subsequent process. Finally, the half cadence (HC) remains categorically distinct from both the authentic cadence categories and the cadential deviations, since its ultimate harmonic goal is dominant (and not tonic) harmony. The HC category also tends to be defined more flexibly than the other categories in that the terminal harmony may support any chord member in the soprano (i.e. 2, 5, or 7).

This study examines three claims about the link between prediction and cadential closure. First, if cadences serve as the most predictable, probabilistic, specifically envisaged formulæ in all of tonal music (Huron, 2006; Meyer, 1956), we would expect terminal events from cadential contexts to be more predictable than those from non-cadential contexts even if both contexts share similar or even identical terminal events (e.g. tonic harmony in root position, 1 in the melody, etc.). Thus, Experiment 1 examines the hypothesis that cadences are more predictable than their non-cadential counterparts by comparing the probability estimates obtained from IDyOM for the terminal events from the PAC and HC categories—the two most prominent categories in tonal music—with those from non-cadential contexts that share identical terminal events.

Second, applications of cadence typologies like the one employed here often note the correspondence between cadential strength (or finality) on the one hand and expectedness (or predictability) on the other. Dunsby has noted, for example, that in Schoenberg’s view, the experience of closure for a given cadential formula is only satisfying to the extent that it fulfils a stylistic expectation (1980, p. 125). This would suggest that the strength and specificity of our schematic expectations

Table 1. The cadential types and categories, along with the harmonic and melodic characteristics and the count for each category in the cadence collection. Categories marked with an asterisk are cadential deviations.
formed in prospect and their subsequent realisation in retrospect contributes to the perception of cadential strength, where the most expected (i.e. probable) endings are also the most complete or closed. Sears (2015) points out that models of cadential strength advanced in contemporary cadence typologies typically fall into two categories: those that compare every cadence category to the perfect authentic cadence (Latham, 2009; Schmalfeldt, 1992), called the 1-schema model; and those that distinguish the PAC, IAC and HC categories from the cadential deviations because the former categories allow listeners to generate expectations as to how they might end, called the Prospective (or Genuine) Schemas model (Sears, 2015, 2016). In the 1-schema model, the half cadence represents the weakest cadential category; it is marked not by a deviation in the melodic and harmonic context at cadential arrival (such as the deceptive or evaded cadences), but rather by the absence of that content, resulting in the following ordering of the cadence categories based on their perceived strength, PAC→IAC→DC→EV→HC. In the Prospective Schemas model, however, the half cadence is a distinct closing schema that allows listeners to generate expectations for its terminal events, and so represents a stronger ending than the aforementioned cadential deviations, resulting in the ordering, PAC→IAC→HC→DC→EV (for further details, see Sears, 2015). Experiment 2 directly compares these two models of cadential strength.

Third, a number of studies have supported the role played by predictive mechanisms in the segmentation of temporal experience (Brent, 1999; Cohen, Adams, & Heeringa, 2007; Elman, 1990; Kurby & Zacks, 2008; Pearce, Müllensiefen, et al., 2010; Peebles, 2011). In event segmentation theory (EST), for example, perceivers form working memory representations of ‘what is happening now,’ called event models, and discontinuities in the stimulus elicit prediction errors that force the perceptual system to update the model and segment activity into discrete time spans, called events (Kurby & Zacks, 2008). In the context of music, such discontinuities can take many forms: sudden changes in melody, harmony, texture, surface activity, rhythmic duration, dynamics, timbre, pitch register, and so on. What is more, when the many parameters affecting segmental grouping act together to produce closure at a particular point in a composition, cadential or otherwise, parametric congruence obtains (Meyer, 1973). Thus, Experiment 3 examines whether (1) the terminal event of a cadence, by serving as a predictable point of closure, is the most expected event in the surrounding sequence; and (2) the next event in the sequence, which initiates the subsequent musical process, is comparatively unexpected. Following EST, the hypothesis here is that unexpected events engender prediction errors that lead the perceptual system to segment the event stream into discrete chunks (Kurby & Zacks, 2008). If the terminal events from genuine cadential contexts are highly predictable, then prediction errors for the comparatively unpredictable events that follow should force listeners to segment the preceding cadential material. For the cadential deviations, however, prediction errors should occur at, rather than following, the terminal events of the cadence.

3. Multiple viewpoints

Most natural languages consist of a finite alphabet of discrete symbols (letters), combinations of which form words, phrases, and so on. As a result, the mapping between the individual letter or word encountered in a printed text and its symbolic representation in a computer database is essentially one-to-one. Music encoding is considerably more complex. Notes, chords, phrases, and the like are characterised by a number of different features, and so regardless of the unit of meaning, digital encodings of individual events must concurrently represent multiple properties of the musical surface. To that end, many symbolic formats employ some variant of the multiple viewpoints framework first proposed by Conklin (1988, 1990) and Conklin and Witten (1995), and later extended and refined by Pearce (2005), Pearce et al. (2005), and Pearce and Wiggins (2004).

The multiple viewpoints framework accepts sequences of musical events that typically correspond to individual notes as notated in a score, but which may also include composite events like chords. Each event e consists of a set of basic attributes, and each attribute is associated with a type, τ, which specifies the properties of that attribute. The syntactic domain (or alphabet) of each type, [τ], denotes the set of all unique elements associated with that type, and each element of the syntactic domain also maps to a corresponding set of elements in the semantic domain, [(τ)]. Following Conklin, attribute types appear here in typewriter font to distinguish them from ordinary text. To represent a sequence of pitches as scale degrees derived from the twelve-tone chromatic scale, for example, the type chromatic scale degree (or csd) would consist of the syntactic set, {0, 1, 2, ..., 11}, and the semantic set, {1, 5/4, 7/5, 2, ..., 7}, where 0 represents 1, 7 represents 5, and so on (see Figure 1).

Within this representation language, Conklin and Witten (1995) define several distinct classes of type, but this study examines just three: basic, derived and linked. Basic types are irreducible representations of the musical surface, which is to say that they cannot be derived from any other type. Thus, an attribute representing the sequence of pitches from the twelve-tone chromatic scale—
domainsofthosetypesdeterminesthe
for any given corpus is that the Cartesian product of the
Indeed,aninterestingpropertyofthesetof
or last events of the melody would receive no value.
would not constitute a basic type because either the first
corpus. For example, a sequence of melodic contours
What is more, basic types represent every event in the
itcannotbederivedfromasequenceofpitchclasses,scale
thefunctionassociatedwithitstype,butforconvenience
elementsoftype
τ


tation,denotedby

therefore denotes the set of all repre-
within attributes, but they fail to represent the relations
attributessuchcadences,forexample,arenecessarilycomprisedofacluster
co-occurringfeatures,soitisimportanttonotenothatthere
relationsbetweenthosefeaturescouldbejustassignif-

4. Finite-context models
4.1. Maximum likelihood estimation
Thegoaloffinite-contextmodelslkeIDyOMistode-
derivefromacorpusofexamplesequenceasmodelestimates
theprobabilityofevent\(e_i\)givingaprecedingsquenceofevents\(e_1\)to\(e_{i-1}\),notatedhereas\(e_{i-1}^1\).Thus,
thefunction\(p(e_i|e_{i-1}^1)\)assumes that theidentityofeach
eventinthesequencedependsonlyontheevents
Itprinciple,thelengthofthectextislimited
context\(e_{i-1}^1\),butcontext
modelstypicallystipulateaglobalorderboundsuchthat
probabilityofthenexteventdependsonlyonthe
previous\(n-1\)events,ormatrix \(p(e_i|e_{(i-n)+1}^1)\).Following
Markovassumption,themodeldescribedhereisan
\(n\)-gramconsistingofacontext\(e_{(i-n)+1}^{i-1}\)andasingle-
eventprediction\(e_i\).

Toestimatetheconditionalprobabilityfunction
\(p(e_i|e_{(i-n)+1}^{i-1})\)foreacheventinthetestsequence,IdyOM
firstacquiresthefrequencycountsforascollectionofsuch
sequencesfromatrainingset.Whenthetrainemodel
isexposedtothetestsequence,ithentousesthefrequency
counts to estimatetheprobabilitydistributiongoverning
theidentityofthenexteventinthesequencegiven
thes\(n-1\)precedingevents(pearce,2005).Inthiscase,IdyOM
reliesonmaximumlikelihood(ML)estimation.

\[
p(e_i|e_{(i-n)+1}^{i-1}) = \frac{c(e_i|e_{(i-n)+1}^{i-1})}{\sum_{e\in A} c(e|e_{(i-n)+1}^{i-1})} \tag{1}
\]

The numerator terms represent the frequency count \(c\)
for the \(n\)-gram \(e_i|e_{(i-n)+1}^{i-1}\), and the denominator terms
representthesumoffreQUENCYcountscarried
with all of the possible events \(e\) in the alphabet \(A\) following
thecontext \(e_{(i-n)+1}^{i-1}\).

---

1Forbasic types like \(c\text{pitch}\), \(\Psi\) is simply a projection function, thereby
returningasoutputthesamevaluesitreceivesasinput(pearce,2005,p.59).

---

**Figure 1.** Top: First violin part from Haydn’s String Quartet in E, Op. 17/1, i, mm. 1–2. Bottom: Viewpoint representation.
4.2. Performance metrics

To evaluate model performance, the most common metrics derive from information-theoretic measures introduced by Shannon (1948, 1951). Returning to Equation 1, if the probability of \( e_i \) is given by the conditional probability function \( p(e_i \mid e_{i-n}^{i-1}) \), information content (IC) represents the minimum number of bits required to encode \( e_i \) in context (MacKay, 2003).

\[
IC(e_i \mid e_{i-n}^{i-1}) = \log_2 \frac{1}{p(e_i \mid e_{i-n}^{i-1})} \tag{2}
\]

IC is inversely proportional to \( p \) and so represents the degree of contextual unexpectedness or surprise associated with \( e_i \). Researchers often prefer to report IC over \( p \) because it has a more convenient scale (\( p \) can become vanishingly small), and since it also has a well-defined interpretation in data compression theory (Pearce, Ruiz et al., 2010), we will prefer it in the analyses that follow.

Whereas IC represents the degree of unexpectedness associated with a particular event \( e_i \) in the sequence, Shannon entropy (\( H \)) represents the degree of contextual uncertainty associated with the probability distribution governing that outcome, where the probability estimates are independent and sum to one.

\[
H(e_{i-n}^{i-1} + 1) = \sum_{e \in A} p(e_i \mid e_{i-n}^{i-1}) IC(e_i \mid e_{i-n}^{i-1}) \tag{3}
\]

\( H \) is computed by averaging the information content over all \( e \) in \( A \) following the context \( e_{i-n}^{i-1} \). According to Shannon’s equation, if the probability of a given outcome is 1, the probabilities for all of the remaining outcomes will be 0, and \( H = 0 \) (i.e. maximum certainty). If all of the outcomes are equally likely, however, \( H \) will be maximum (i.e. maximum uncertainty). Thus, one can assume that the best performing models will minimise uncertainty.

In practice, we rarely know the true probability distribution of the stochastic process (Pearce & Wiggins, 2004), so it is often necessary to evaluate model performance using an alternative measure called cross entropy, denoted by \( H_m \).

\[
H_m(p_m, e_i^j) = -\frac{1}{j} \sum_{i=1}^{j} \log_2 p_m(e_i \mid e_1^{i-1}) \tag{4}
\]

Whereas \( H \) represents the average information content over all \( e \) in the alphabet \( A \), \( H_m \) represents the average information content for the model probabilities estimated by \( p_m \) over all \( e \) in the sequence \( e_1^j \). That is, cross entropy provides an estimate of how uncertain a model is, on average, when predicting a given sequence of events (Manning & Schütze, 1999; Pearce & Wiggins, 2004). As a consequence, \( H_m \) is often used to evaluate the performance of context models for tasks like speech recognition, machine translation, and spelling correction because, as Brown and his co-authors put it, ‘models for which the cross entropy is lower lead directly to better performance’ (Brown, Della Pietra, Della Pietra, Lai, & Mercer, 1992, p. 39).

4.3. Prediction by Partial Match

Because the number of potential patterns decreases dramatically as the value of \( n \) increases, high-order models often suffer from the zero-frequency problem, in which \( n \)-grams encountered in the test set do not appear in the training set (Witten & Bell, 1991). To resolve this issue, IDyOM applies a data compression scheme called Prediction by Partial Match (PPM), which adjusts the ML estimate for each event in the sequence by combining (or smoothing) predictions generated at higher orders with less sparsely estimated predictions from lower orders (Cleary & Witten, 1984). Context models estimated with the PPM scheme typically use a procedure called backoff smoothing (or blending), which assigns some portion of the probability mass from each distribution to an escape probability using an escape method to accommodate predictions that do not appear in the training set. When a given event does not appear in the \( n - 1 \) order distribution, PPM stores the escape probability and then iteratively backs off to lower order distributions until it predicts the event or reaches the zeroth-order distribution, at which point it transmits the probability estimate for a uniform distribution over \( A \) (i.e. where every event in the alphabet is equally likely). PPM then multiplies these probability estimates together to obtain the final (smoothed) estimate.

Unfortunately there is no sound theoretical basis for choosing the appropriate escape method (Witten & Bell, 1991), but two recent studies have demonstrated the potential of Moffat’s (1990) method C to minimise model uncertainty in melodic and harmonic prediction tasks (Hedges & Wiggins, 2016; Pearce & Wiggins, 2004), so we employ that method here.

\[
\gamma(e_{i-n}^{i-1} + 1) = \frac{t(e_{i-n}^{i-1} + 1)}{\sum_{e \in A} c(e_{i-n}^{i-1} + 1) + t(e_{i-n}^{i-1} + 1)} \tag{5}
\]

Escape method C represents the escape count \( t \) as the number of distinct symbols that follow the context \( e_{i-n}^{i-1} + 1 \). To calculate the escape probability for events that do not appear in the training set, \( y \) represents
the ratio of the escape count \( t \) to the sum of the frequency counts \( c \) and \( t \) for the context \( e_{(i-n)+1} \). The appeal of this escape method is that it assigns greater weighting to higher-order predictions (which are more specific to the context) over lower order predictions (which are more general) in the final probability estimate (Bunton, 1996; Pearce, 2005). Thus, Equation 1 can be revised in the following way:

\[
\alpha(e_i|e_{(i-n)+1}) = \frac{c(e_{i}|e_{(i-n)+1})}{\sum_{e \in A} c(e_{i}|e_{(i-n)+1}) + t(e_{i}|e_{(i-n)+1})} \quad (6)
\]

The PPM scheme just described remains the canonical method in many context models (Cleary & Teahan, 1997), but Bunton (1997) has since provided a variant smoothing technique called mixtures that generally improves model performance, but which, following Chen and Goodman (1999), we refer to as interpolated smoothing (Pearce & Wiggins, 2004). The central idea behind interpolated smoothing is to compute a weighted combination of higher order and lower order models for every event in the sequence—regardless of whether that event features \( n \)-grams with zero-counts—under the assumption that the addition of lower order models might generate more accurate probability estimates.\(^2\)

Formally, interpolated smoothing estimates the probability function \( p(e_i|e_{(i-n)+1}) \) by recursively computing a weighted combination of the \((n-1)\)th order distribution with the \((n-2)\)th order distribution (Pearce, 2005; Pearce & Wiggins, 2004).

\[
p(e_i|e_{(i-n)+1}) = \begin{cases} \alpha(e_i|e_{(i-n)+1}) + \gamma(e_{i-n+1})p(e_i|e_{(i-n)+2}) & \text{if } e_{(i-n)+2} \neq \varepsilon \\ \frac{1}{|A|+1-n(e)} & \text{otherwise} \end{cases} \quad (7)
\]

In the context of interpolated smoothing, it can be helpful to think of \( \gamma \) as a weighting function, with \( \alpha \) serving as the weighted ML estimate. Unlike the backoff smoothing procedure, which terminates at the first non-zero prediction, interpolated smoothing recursively adjusts the probability estimate for each order—regardless of whether the corresponding \( n \)-gram features a non-zero count—and then terminates with the probability estimate for \( \varepsilon \), which represents a uniform distribution over \(|A|+1-n(e)\) events (i.e. where every event in the alphabet is equally likely). Also note here that in the PPM scheme, the alphabet \( A \) increases by one event to accommodate the escape count \( t \) but decreases by the number of events in \( A \) that never appear in the corpus.\(^3\)

### 4.4. Variable orders

The optimal order for context models depends on the nature of the corpus, which in the absence of a priori knowledge can only be determined empirically (2004, p. 2). To resolve this issue, IDyOM employs an extension to PPM called PPM* (Cleary & Teahan, 1997), which includes contexts of variable length and thus ‘eliminates the need to impose an arbitrary order bound’ (Pearce & Wiggins, 2004, p. 6). In the PPM* scheme, the context length is allowed to vary for each event in the sequence, with the maximum context length selected using simple heuristics to minimise model uncertainty. Specifically, PPM* exploits the fact that the observed frequency of novel events is much lower than expected for contexts that feature exactly one prediction, called deterministic contexts. As a result, the entropy of the distributions estimated at or below deterministic contexts tends to be lower than in non-deterministic contexts. Thus, PPM* selects the shortest deterministic context to serve as the global order bound for each event in the sequence. If such a context does not exist, PPM* then selects the longest matching context.

### 5. Methods

#### 5.1. The corpus

The corpus consists of symbolic representations of 50 sonata-form expositions selected from Haydn’s string quartets (1771–1803). Table 2 presents the reference information, keys, time signatures and tempo markings for each movement. The corpus spans much of Haydn’s mature compositional style (Opp. 17–76), with the majority of the expositions selected from first movements (28) or finales (11), and with the remainder appearing in inner movements (ii: 8; iii: 3). All movements were downloaded from the KernScores database in MIDI format.\(^4\)

To ensure that each instrumental part would qualify as monophonic—a pre-requisite for the analytical techniques that follow—all trills, extended string techniques, and other ornaments were removed. For events presenting extended string techniques (e.g. double or triple stops), note events in each part were retained that preserved the voice leading both within and between instrumental parts. Table 3 provides a few descriptives concerning the number of note and chord events in each movement.

---

\(^2\)Context models like the one just described also often use a technique called exclusion, which improves the final probability estimate by retracting a portion of the probability mass in lower order models that is otherwise wasted on redundant predictions (i.e. the counts for events that were predicted in the higher-order distributions do not need to be included in the calculation of the lower order distributions).

\(^3\)For a worked example of the PPM* method, see Sears (2016).

\(^4\)http://kern.ccarh.org/.
Table 2. Reference information (Opus number, work, movement, measures), keys (case denotes mode), time signatures and tempo markings for the exposition sections in the corpus.

<table>
<thead>
<tr>
<th>Excerpt</th>
<th>Key</th>
<th>Time signature</th>
<th>Tempo marking</th>
</tr>
</thead>
<tbody>
<tr>
<td>Op. 17, No. 1, i, mm. 1–43</td>
<td>E</td>
<td>4/4</td>
<td>Moderato</td>
</tr>
<tr>
<td>Op. 17, No. 2, i, mm. 1–38</td>
<td>F</td>
<td>4/4</td>
<td>Moderato</td>
</tr>
<tr>
<td>Op. 17, No. 3, iv, mm. 1–26</td>
<td>E♭</td>
<td>4/4</td>
<td>Allegro molto</td>
</tr>
<tr>
<td>Op. 17, No. 4, i, mm. 1–53</td>
<td>c</td>
<td>4/4</td>
<td>Moderato</td>
</tr>
<tr>
<td>Op. 17, No. 6, i, mm. 1–73</td>
<td>D</td>
<td>6/8</td>
<td>Presto</td>
</tr>
<tr>
<td>Op. 20, No. 1, iv, mm. 1–55</td>
<td>E♭</td>
<td>2/4</td>
<td>Allegro con spirito</td>
</tr>
<tr>
<td>Op. 20, No. 3, i, mm. 1–94</td>
<td>g</td>
<td>2/4</td>
<td>Allegro</td>
</tr>
<tr>
<td>Op. 20, No. 3, iii, mm. 1–43</td>
<td>G</td>
<td>3/4</td>
<td>Poco Adagio</td>
</tr>
<tr>
<td>Op. 20, No. 3, iv, mm. 1–42</td>
<td>g</td>
<td>4/4</td>
<td>Allegro molto</td>
</tr>
<tr>
<td>Op. 20, No. 4, i, mm. 1–49</td>
<td>D</td>
<td>4/4</td>
<td>Allegro moderato</td>
</tr>
<tr>
<td>Op. 20, No. 5, i, mm. 1–48</td>
<td>f</td>
<td>4/4</td>
<td>Allegro</td>
</tr>
<tr>
<td>Op. 20, No. 6, ii, mm. 1–27</td>
<td>E</td>
<td>cut</td>
<td>Adagio</td>
</tr>
<tr>
<td>Op. 33, No. 1, i, mm. 1–37</td>
<td>b</td>
<td>4/4</td>
<td>Allegro moderato</td>
</tr>
<tr>
<td>Op. 33, No. 1, iii, mm. 1–40</td>
<td>D</td>
<td>6/8</td>
<td>Andante</td>
</tr>
<tr>
<td>Op. 33, No. 2, i, mm. 1–32</td>
<td>E♭</td>
<td>4/4</td>
<td>Allegro moderato</td>
</tr>
<tr>
<td>Op. 33, No. 3, iii, mm. 1–29</td>
<td>F</td>
<td>3/4</td>
<td>Adagio</td>
</tr>
<tr>
<td>Op. 33, No. 4, iv, mm. 1–31</td>
<td>B♭</td>
<td>4/4</td>
<td>Allegro moderato</td>
</tr>
<tr>
<td>Op. 33, No. 5, i, mm. 1–95</td>
<td>G</td>
<td>2/4</td>
<td>Vivace assai</td>
</tr>
</tbody>
</table>
| Op. 33, No. 5, ii, mm. 1–30 | g |indicated in Table 1. The corpus contains 270 cadences, but 15 cadences were excluded because either the cadential bass or soprano does not appear in the cello and first violin parts, respectively. Additionally, another 10 cadences were excluded because they imply more than one category (i.e. PAC–EV or DC–EV). Thus, for the analyses that follow, the cadence collection consists of 245 cadences.

To examine model predictions for the cadences in the corpus, we classified exemplars of the five cadence categories that achieve (or at least promise) cadential arrival in Caplin’s cadence typology—PAC, IAC, HC, DC and EV (see Table 1). The corpus contains 270 cadences, but 15 cadences were excluded because either the cadential bass or soprano does not appear in the cello and first violin parts, respectively. Additionally, another 10 cadences were excluded because they imply more than one category (i.e. PAC–EV or DC–EV). Thus, for the analyses that follow, the cadence collection consists of 245 cadences.

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Shown in the right-most column of Table 1, the perfect authentic cadence and the half cadence represent the most prevalent categories, followed by the caden-
tial deviations: the deceptive and evaded categories. The imperfect authentic cadence is the least common category, which perhaps reflects the late-century stylistic preference for perfect authentic cadential closure at the ends of themes and larger sections. This distribution also largely replicates previous findings for Mozart’s keyboard sonatas (Rohrmeier & Neuwirth, 2011), so it is possible that this distribution may characterise the classical style in general.

5.2. Viewpoint selection

To select the appropriate viewpoints for the prediction of cadences in Haydn’s string quartets, we have adopted Gjerdingen’s schema-theoretic approach (2007), which represents the ‘core’ events of the cadence by the scale degrees and melodic contours of the outer voices (i.e. the two-voice framework), a coefficient representing the strength of the metric position (strong, weak), and a sonority, presented using figured bass notation. Given the importance of melodic intervals in studies of recognition memory for melodies (Dowling, 1981) we might also add this attribute to Gjerdingen’s list. However, for the majority of the encoded cadences from the cadence collection, the terminal events at the moment of cadential arrival appear in strong metric positions, and few of the cadences feature unexpected durations or inter-onset intervals at the cadential arrival, so we have excluded viewpoint models for rhythmic or metric attributes from the present investigation, concentrating instead on those viewpoints representing pitch-based (melodic or harmonic) expectations. What is more, IDyOM was designed to combine melodic predictions from two or more viewpoints by mapping the probability distributions over their respective alphabets back into distributions over a single basic viewpoint, such as the pitches of the twelve-tone chromatic scale (i.e. cpitch). Thus, for the purposes of model comparison it will also be useful to include cpitch as a baseline melodic model in the analyses that follow.

5.2.1. Note events

Four viewpoints were initially selected to represent note events in the outer parts: chromatic pitch (cpitch), melodic pitch interval (melint), melodic contour (contour), and chromatic scale degree (csd). As described previously, cpitch represents pitches as integers from 0–127 (in the MIDI representation, C4 is 60), and serves as the baseline model for the other melodic viewpoint models examined in this study. To derive sequences of melodic intervals, melint computes the numerical difference between adjacent events in cpitch, where ascending intervals are positive and descending intervals are negative. The viewpoint contour then reduces the information present in melint, with all ascending intervals receiving a value of 1, all descending intervals a value of −1, and all lateral motion a value of 0. Finally, to relate cpitch to a referential tonic pitch class for every event in the corpus, we manually annotated the key, mode, modulations and pivot boundaries for each movement and then included the analysis in a separate text file to accompany the MIDI representation, both of which appear in the Supplementary materials for each movement in the corpus. Thus, every note event was associated with the viewpoints key and mode. The vector of keys assumes values in the set {0, 1, 2, ..., 11}, where 0 represents the key of C, 1 represents C♯ or Db, and so on. Passages in the major and minor modes receive values of 0 and 1, respectively. The viewpoint csd then maps cpitch to key and reduces the resulting vector of chromatic scale degrees modulo 12 such that 0 denotes the tonic scale degree, 7 the dominant scale degree, and so on. By way of example, Figure 1 presents the viewpoint representation for the first violin part from the opening two measures of the first movement of Haydn’s String Quartet in E, Op. 17/1.

As mentioned previously, IDyOM is capable of individually predicting any one of these viewpoints using the PPM* scheme, but it can also combine viewpoint models for note-event predictions of the same basic viewpoint (i.e. cpitch) using a weighted multiplicative combination scheme that assigns greater weights to viewpoints whose predictions are associated with lower entropy at that point in the sequence (Pearce et al., 2005). To determine the combined probability distribution for each event in the test sequence, IDyOM then computes the product of the weighted probability estimates from each viewpoint model for each possible value of the predicted viewpoint.

Furthermore, IDyOM can automate the viewpoint selection process using a hill-climbing procedure called forward stepwise selection, which picks the combination of viewpoints that yields the richest structural representations of the musical surface and minimises model uncertainty. Given an empty set of viewpoints, the stepwise selection algorithm iteratively selects the viewpoint model additions or deletions that yield the most improvement in cross entropy, terminating when no addition or deletion yields an improvement (Pearce, 2005; Potter, Wiggins, & Pearce, 2007). To derive the optimal viewpoint system for the representation of melodic expectations, we employed stepwise selection for the following viewpoints: cpitch, melint, csd, and contour. In this case, IDyOM begins with the above set of viewpoint models, but also includes the linked viewpoints derived from that set (i.e. cpitch ⊗ melint,
combination (two instrumental parts is 133 possible classes, so the number of combinatorial possibilities for combinations containing two, three, or four instrumental parts is $13^3 - 1$, or 2196 combinations.

To reduce the syntactic domain while retaining those viewpoint models for the first violin and the cello. For this corpus, melint was the best performing viewpoint model in the first step, receiving a cross entropy estimate of 3.006 in the first violin and 2.798 in the cello. In the second step, the combination of melint with the linked viewpoint cpitch decreased the cross entropy estimate to 2.765 in the first violin and 2.556 in the cello. Including any of the remaining viewpoints did not improve model performance, so the stepwise selection procedure terminated with this combination of viewpoints. In Section 6, we refer to this viewpoint model as selection. What is more, the contour model received a much higher cross entropy estimate than the other viewpoint models, so we elected to exclude it in the experiments reported here. Thus, the final melodic viewpoint models selected for the present study are cpitch, melint, csdc, and selection.

5.2.2. Chord events

To accommodate chord events, we have extended the multiple viewpoints framework by performing a full expansion of the symbolic encoding, which duplicates overlapping note events across the instrumental parts at every unique onset time (Conklin, 2002). This representation yielded two harmonic viewpoints: vertical interval class combination (vintcc) and chromatic scale-degree combination (csdc). The viewpoint vintcc produces a sequence of chords that have analogues in figured-bass nomenclature by modelling the vertical intervals in semitones modulo 12 between the lowest instrumental part and the upper parts from cpitch. Unfortunately, however, the syntactic domain of vintcc is rather large; the domain of each vertical interval class between any two instrumental parts is $\{0, 1, 2, \ldots, 11, \bot\}$, yielding 13 possible classes, so the number of combinatorial possibilities for combinations containing two, three, or four instrumental parts is $13^3 - 1$, or 2196 combinations.

To reduce the syntactic domain while retaining those chord combinations that approximate figured bass symbols, Quinn (2010) assumed that the precise location and repeated appearance of a given interval in the instrumental texture are inconsequential to the identity of the combination. Adopting that approach here, we have excluded note events in the upper parts that double the lowest instrumental part at the unison or octave, allowed permutations between vertical intervals, and excluded interval repetitions. As a consequence, the first two criteria reduce the major triads $\langle 4, 7, 0 \rangle$ and $\langle 7, 4, 0 \rangle$ to $\langle 4, 7, \bot \rangle$, while the third criterion reduces the chords $(4, 4, 10)$ and $(4, 10, 10)$ to $(4, 10, \bot)$. This procedure dramatically reduces the potential domain of vintcc from 2196 to 232 unique vertical interval class combinations, though the corpus only contained 190 of the 232 possible combinations, reducing the domain yet further.

To relate each combination to an underlying harmonic viewpoint, csdc represents vertical sonorities as combinations of chromatic scale degrees that are intended to approximate Roman numerals. The viewpoint csdc includes the chromatic scale degrees derived from csd as combinations of two, three or four instrumental parts. Here, the number of possibilities increases exponentially to $13^4 - 13^3$, or 28,548 combinations, since the cello part is now encoded explicitly in combinations containing all four parts. Rather than treating permutable combinations as equivalent (e.g. $(0, 4, 7, \bot)$ and $(4, 7, 0, \bot)$), as was done for vintcc, it will also be useful to retain the chromatic scale degree in the lowest instrumental part in csdc and only permit permutations in the upper parts. Excluding voice doublings and permitting permutations in the upper parts reduces the potential domain of csdc to 2784, though in the corpus the domain reduced yet further to 688 distinct combinations.

Finally, a composite viewpoint was also created to represent those viewpoint models characterising pitch-based (i.e. melodic and harmonic) expectations more generally. To simulate the cognitive mechanisms underlying melodic segmentation, Pearce, Müllensiefen, et al. (2010) found it beneficial to combine viewpoint predictions for basic attributes like chromatic pitch, inter-onset interval, and offset-to-onset interval by multiplying the component probabilities to reach an overall probability for each note in the sequence as the joint probability of the individual basic attributes being predicted. Following their approach, the viewpoint model composite represents the product of the selection viewpoint model from the first violin (to represent melodic expectations) and the csdc viewpoint model (to represent harmonic expectations) for each unique onset time for which a note and chord event appear in the corpus. In this case, csdc was preferred to vintcc in the composite model because the former viewpoint explicitly encodes the chromatic scale-degree successions in the lowest instrumental part along with the relevant scale degrees from the upper parts.

5.3. Long-term vs. short-term

To improve model performance, IDyOM separately estimates and then combines two subordinate models trained on different subsets of the corpus for each view-
point: a long-term model (LTM), which is trained on the entire corpus to simulate long-term, schematic knowledge; and a short-term model (STM), which is initially empty for each individual composition and then is trained incrementally to simulate short-term, dynamic knowledge (Pearce & Wiggins, 2012). As a result, the long-term model reflects inter-opus statistics from a large corpus of compositions, whereas the short-term model only reflects intra-opus statistics, some of which may be specific to that composition (Conklin & Witten, 1995; Pearce & Wiggins, 2004). Like the STM, the LTM may also be slightly improved by incrementally training on the composition being predicted, called LTM+. However, the STM only discards statistics when it reaches the end of the composition, so it far surpasses the supposed upper limits for short-term and working memory of around 10–12 s (Snyder, 2000), sometimes by several minutes. What is more, the STM should be irrelevant for the present purposes, since cadences exemplify the kinds of inter-opus patterns that listeners are likely to store in long-term memory. Thus, we have elected to omit the STM in the analyses that follow and only present the probability estimates from LTM+.

5.4. Performance evaluation

Context models like IDyOM depend on a training set and a test set, but in this case the corpus will need to serve as both. To accommodate small corpora like this one, IDyOM employs a resampling approach called k-fold cross-validation (Dietterich, 1998), using cross entropy as a measure of performance (Conklin & Witten, 1995). The corpus is divided into k disjoint subsets containing the same number of compositions, and the LTM+ is trained k times on k – 1 subsets, each time leaving out a different subset for testing. IDyOM then computes an average of the k cross entropy values as a measure of the model’s performance. Following Pearce and Wiggins (2004), we use 10-fold cross validation for the models that follow.

6. Computational experiments

6.1. Experiment 1

The perfect authentic and half cadence categories account for 206 of the 245 cadences from the collection, so it seems reasonable that listeners with sufficient exposure to music of the classical style will form schematic expectations for the terminal events of exemplars from these two categories. What is more, if cadences are the most predictable formulæ in all of tonal music, we should expect to find lower IC estimates for the terminal events from the aforementioned cadence categories compared to those from non-cadential closing contexts even if they both share similar or even identical terminal events. Thus, Experiment 1 examines the hypothesis that cadences are more predictable than their non-cadential counterparts.

6.1.1. Analysis

To compare the PAC and HC categories against non-cadential contexts exhibiting varying degrees of closure or stability, each of the viewpoints estimated by IDyOM was analysed for the terminal note events from the first violin and cello — represented by the viewpoints cpitch, melint, csd, and selection — and the terminal chord events from the entire texture — represented by the viewpoints vintcc, csdcc, and composite — using a one-way analysis of variance (ANOVA) with a three-level between-groups factor called closure. To examine the IC estimates for the first (tonic) type, tonic closure consists of three levels: PAC, which consists of the IC estimates for the terminal events from the 122 exemplars of the PAC category; tonic, which consists of an equal-sized sample of events selected randomly from the corpus that appear in strong metric positions (i.e. appearing at the tactus level; see Sears, 2016) and feature tonic harmony in root position and any scale degree in the soprano; and nontonic, which again consists of an equal-sized sample of events selected randomly from the corpus that appear in strong metric positions, but that feature any other harmony and any other scale degree in the soprano. To compare the PAC and HC categories against non-cadential views, each of the viewpoints estimated by IDyOM — and the terminal chord events from the entire texture — represented by the viewpoints cpitch, melint, and cello — represented by the viewpoints cpitch, melint, and cello — using a one-way analysis of variance (ANOVA) with a three-level between-groups factor called closure. To examine the IC estimates for the second (dominant) type, dominant closure was designed in much the same way. HC consists of the IC estimates for the terminal events from the 84 exemplars of the HC category, while the other two levels consist of equal-sized samples of non-cadential events selected at random. Events from dominant appear in strong metric positions and feature dominant harmony in root position with any scale degree in the soprano, while events from other appear in strong metric positions but exclude events featuring tonic or dominant harmonies in root position. The assumption behind this additional exclusion criterion is that tonic events in root position are potentially more predictable than root-position dominants in half-cadential contexts (an assumption examined in greater detail in Experiment 2), so it was necessary here to provide a condition that allows us to compare the IC estimates for the terminal events in half-cadential contexts against those featuring other, presumably less stable harmonies and scale degrees.

For every between-groups factor examined in the experiments reported here, Levene’s equality of variances revealed significant differences between groups for nearly every viewpoint model. Thus, we employ an alternative to Fisher’s F ratio that is generally robust to heteroscedastic
data, called the Welch F ratio (Welch, 1951). To determine the effect size both for the Welch F ratio and for the planned comparisons described shortly, we use Cohen's (2008) recent notation of a common effect size measure called estimated $\omega^2$.

To address more specific hypotheses about the potential differences in the IC estimates for the terminal events from cadential and non-cadential contexts, each model also includes two planned comparisons that do not assume equal variances: the first to determine whether the IC estimates from the corresponding cadence category differ significantly from the two non-cadential levels (Cadences vs. Non-Cadences), and the second to determine whether the IC estimates from the corresponding cadence category differ significantly from the second (tonic or dominant) level of closure (PAC vs Historic or HC vs. Dominant). Unfortunately, these additional tests increase the risk of committing a Type I error, so we apply Bonferroni correction to the planned comparisons.

### 6.1.2. Results

The top bar plots in Figure 2 display the mean IC estimates for the terminal note event in the first violin (left) and cello (right) for each level of tonic closure. Table 4 presents the omnibus statistics and planned comparisons. Beginning with the first violin, one-way ANOVAs of the IC estimates revealed a main effect for the viewpoints melint, csd, and the optimised combination selection, but the baseline viewpoint, cpitch, was not significant. Mean IC estimates also increased significantly from PAC to the non-cadential levels of tonic closure for melint, csd, and selection. Although this trend also emerged for the second planned comparison between PAC and tonic, only the melint model revealed a significant effect. Thus, the viewpoint models for the first violin demonstrated that terminal note events from cadential contexts are more predictable than those from non-cadential contexts.

For the cello, one-way ANOVAs revealed a main effect of tonic closure for every viewpoint, but the direction of the effect was reversed. Mean IC estimates decreased in every model from PAC to the non-cadential levels of tonic closure, as well as from PAC to tonic. Thus, contrary to our predictions, the terminal events in the cello from cadential contexts were actually less predictable than those from non-cadential contexts.

The bottom-left bar plot in Figure 2 displays the mean IC estimates for the terminal chord event—represented by vintcc and csdc—for each level of the between-groups factor. One-way ANOVAs again revealed a main effect of tonic closure for vintcc and csdc, with the mean IC estimates increasing from PAC to the non-cadential levels of tonic closure. The second planned comparison comparing PAC to tonic was not significant for either viewpoint model, however. Thus, for both models the terminal chord events from cadential contexts were more predictable than those from non-cadential contexts.

To represent the predictability of the harmony and melody in a single IC estimate for each note/chord event, we created a composite viewpoint that reflects the joint probability of csdc and selection$_{IH}$. The bottom-right line plot in Figure 2 displays the mean IC estimates for the terminal composite event for each level of tonic closure. In this case, the one-way ANOVA revealed a significant main effect, with the mean IC estimates increasing from PAC to the non-cadential levels of closure, and the increase from PAC to tonic was marginally significant. As a result, composite demonstrated an ascending staircase for the levels of tonic closure, with PAC receiving the lowest IC estimates and non-tonic receiving the highest IC estimates.

The top bar plots in Figure 3 display the mean IC estimates for the terminal note event in the first violin (left) and cello (right) for each level of dominant closure. Table 5 presents the omnibus statistics and planned comparisons. For the first violin, one-way ANOVAs revealed a main effect for every viewpoint model. As expected, the mean IC estimates also increased significantly from HC to the non-cadential levels of dominant closure for every model. The increase from HC to dominant was also significant for cpitch, melint, and selection, but not for csd.

For the cello, the mean IC estimates demonstrated a significant effect of dominant closure for csd, but the other viewpoint models were not significant. For csd, the mean IC estimates increased significantly from HC to the non-cadential levels. A similar trend also emerged for the second planned comparison between HC and dominant, but the effect was not significant. For the viewpoint models representing harmonic progressions, the mean IC estimates revealed main effects of dominant closure for vintcc and csdc, suggesting that the terminal note and chord events represented in the cello and the entire multi-voiced texture are more predictable in half-cadential contexts than in non-cadential contexts. The first planned comparison comparing HC with the two non-cadential levels was not significant for these viewpoint models, however. Finally, the composite viewpoint demonstrated a significant main effect of dominant closure, with the mean IC estimates increasing significantly from HC to the non-cadential levels, but not from HC to dominant.

### 6.1.3. Discussion

Both between-groups factors demonstrated significantly lower mean IC estimates for the terminal events from
cadential contexts compared to those from non-cadential contexts. The factor tonic closure elicited significant effects for viewpoints representing both voices of the two-voice framework, with greater effect sizes appearing for viewpoint models characterising harmonic progressions (vintcc, csdc, and composite). For viewpoint models representing the cello explicitly, however, the terminal events from perfect authentic cadential contexts were actually less predictable than those from non-cadential tonic contexts. This finding may reflect limitations of the modelling approach (see Section 7), but since the leap in the bass by descending fifth (or ascending fourth) in perfect authentic cadential contexts occurs less frequently than motion by smaller intervals in any other context (e.g. by unison, m2, or M2) (Sears, 2016), it may also be that cadential bass lines are simply less predictable than their stepwise, non-cadential counterparts when considered in isolation. For the viewpoints that explicitly model the interaction between the bass and the upper voices, however (e.g. vintcc, csdc, or composite), IDyOM produced considerably lower IC estimates for cadential successions like $\hat{5}$-$\hat{1}$ than for non-cadential successions like $\hat{1}$-$\hat{1}$, $\hat{2}$-$\hat{1}$, or $\hat{7}$-$\hat{1}$.
For **dominant closure**, significant effects were generally limited to the viewpoint models for csd in the outer parts, but the effects were more pronounced for the csdc and composite models. In each case, the terminal events from cadential contexts were more predictable than those from non-cadential contexts. Nevertheless, half-cadential contexts generally failed to elicit lower mean IC estimates compared to non-cadential root-position dominants. Thus, according to IDyOM, the terminal events from the HC level are no more (or less) predictable than any other instance of root-position dominant harmony selected at random from the corpus.

Given our earlier assumptions about schematic expectations for dominant events, these results should not be surprising. Nevertheless, it remains unclear whether terminal events from half cadences receive higher IC estimates on average due to limitations of the modelling approach, because the preceding context fails to stimulate strong expectations for any particular continuation, or because the actual continuation is unexpected (Pearce, Müllensiefen, et al., 2010, pp. 1374–1375). And yet, by only considering the potential differences between cadential and non-cadential contexts, the previous analysis failed to directly compare the cadence categories from

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**Table 5.** Analysis of variance and planned comparisons predicting the information content estimates from all viewpoint models with dominant closure.

<table>
<thead>
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<th>Viewpoint</th>
<th>df</th>
<th>Welch F</th>
<th>est. ω²</th>
<th>p</th>
<th>df</th>
<th>t</th>
<th>r</th>
<th>p</th>
<th>df</th>
<th>t</th>
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<td>.26</td>
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<td>−4.26</td>
<td>.28</td>
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<tr>
<td>cpitch</td>
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<td>≈ 0</td>
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<td>NS</td>
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<td>0.94</td>
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<td>16.66</td>
<td>.08</td>
<td>&lt;.001</td>
<td>216.71</td>
<td>−1.42</td>
<td>.09</td>
<td>NS</td>
<td>160.57</td>
<td>2.45</td>
<td>.16</td>
<td>NS</td>
</tr>
<tr>
<td>csd</td>
<td>164.84</td>
<td>4.00</td>
<td>.02</td>
<td>.020</td>
<td>187.47</td>
<td>−1.86</td>
<td>.12</td>
<td>NS</td>
<td>165.37</td>
<td>0.36</td>
<td>.02</td>
<td>NS</td>
</tr>
<tr>
<td>composite</td>
<td>162.93</td>
<td>8.04</td>
<td>.04</td>
<td>&lt;.001</td>
<td>203.00</td>
<td>−3.56</td>
<td>.24</td>
<td>&lt;.001</td>
<td>163.99</td>
<td>−1.74</td>
<td>.13</td>
<td>NS</td>
</tr>
</tbody>
</table>

Note: NS = non-significant. Planned comparisons corrected with Bonferroni adjustment.
Caplin’s typology. We might hypothesise, for example, that the strength and specificity of our schematic expectations formed in prospect and their subsequent realisation in retrospect contributes to the perception of cadential strength, where the most expected (i.e. probable) endings are also the most complete or closed. From this point of view, the probabilities estimated by IDyOM might correspond with models of cadential strength advanced in contemporary cadence typologies.

### 6.2. Experiment 2

Recall that the cadence collection consists of exemplars from five categories in Caplin’s typology: PAC, IAC, HC, DC, and EV. Sears (2015) recently classified models that estimate the closural strength of these categories into two general types: those that relate every cadential category to one essential prototype, called the 1-Schema model (Latham, 2009; Schmalfeldt, 1992); and those that distinguish the categories according to whether they allow listeners to form expectations as to how they might end, called the Prospective Schemas model (Sears, 2015) (see Section 2). Experiment 2 directly compares these two models of cadential strength.

#### 6.2.1. Analysis

To compare the mean IC estimates for the terminal events from each cadence category, each of the viewpoints was again analysed for the terminal note events from the first violin and cello and the terminal chord events from the entire texture using a one-way ANOVA with a five-level between-groups factor called cadence category (PAC, IAC, HC, DC, and EV). To examine the potential differences in the IC estimates for the terminal events from each cadence category, each model includes two planned comparisons that do not assume equal variances, with a Bonferroni correction applied to the obtained statistics. In the first comparison, each level of cadence category was coded to represent two models of cadential strength: Prospective Schemas (PAC→IAC→HC→DC→EV) and 1-Schema (PAC→IAC→DC→EV→HC). Polynomial contrasts with linear and quadratic terms were then included to estimate the goodness-of-fit for each model. In what follows, we report the contrast whose linear or quadratic trend accounts for the greatest proportion of variance in the outcome variable. The second comparison examines the hypothesis that the genuine cadence categories in Caplin’s typology elicit lower IC estimates on average than the cadential deviations (Genuine vs. Deviations).

#### 6.2.2. Results

Figure 4 displays line plots of the mean IC estimates for the terminal note event in the first violin (left) and cello (right) for each level of cadence category. Table 6 presents the omnibus statistics and planned comparisons. For the first violin, the mean IC estimates revealed a main effect for the viewpoints $cpitch$, $csd$, and $selection$, but not for melint. Moreover, the best-fitting polynomial contrast revealed a positive (increasing) linear trend in the Prospective Schemas model (i.e. from the PAC to the EV categories) for every viewpoint model. The genuine cadence categories also received lower mean IC estimates than the cadential deviations in every model.

For the cello, the IC estimates also revealed a main effect of cadence category for every viewpoint model, and the Prospective Schemas model again produced the best fit, with polynomial contrasts revealing positive quadratic trends for $cpitch$ and melint, but positive linear trends for $csd$ and $selection$. The quadratic trend exhibited in the $cpitch$ and melint models for the cello probably reflects the statistical preference for smaller melodic intervals in the corpus, resulting in lower mean IC estimates for categories that feature stepwise successions like $\hat{5}$–$\hat{1}$. And yet successions like $\hat{5}$–$\hat{6}$ are more common than successions like $\hat{5}$–$\hat{1}$, hence the higher IC estimates for the DC category and the increasing linear trend, $PAC→IAC→DC→EV$. Finally, as expected, the genuine cadence categories received lower mean IC estimates than the cadential deviations in every model.

The left line plot in Figure 5 displays the mean IC estimates for the terminal chord event—represented by vintcc and csdcc—for each level of cadence category. As before, the IC estimates revealed a main effect for vintcc and csdcc, and the best-fitting polynomial contrast revealed a positive linear trend in the Prospective Schemas model for both models. The genuine cadence categories also received lower mean IC estimates than the cadential deviations for vintcc and csdcc.

It is also noteworthy that the terminal events from the EV category generally received lower IC estimates than those from the DC category. Recall that evaded cadences are typically characterised not by a deviation in the harmonic progression (though such a deviation may take place), but rather by a sudden interruption in the projected resolution of the melody. In this collection, 10 of the 11 evaded cadences feature tonic harmony either in root position or in first inversion at the moment of
Figure 4. Line plots of the mean IC estimated for the terminal note event in the first violin (left) and cello (right) for each cadence category. Viewpoints include cpitch, melint, csd, and an optimised combination called selection, which represents melint and the linked viewpoint csd ⊗ cpitch. Whiskers represent ±1 standard error.

Table 6. Analysis of variance and planned comparisons predicting the information content estimates from all viewpoint models with cadence categories.

<table>
<thead>
<tr>
<th>Viewpoint</th>
<th>df</th>
<th>Welch F</th>
<th>est. $\omega^2$</th>
<th>p</th>
<th>Omnibus Comparisons</th>
<th>Prospective Schemas</th>
<th>Genuine vs. Deviations</th>
</tr>
</thead>
<tbody>
<tr>
<td>Note events</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Violin 1</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>cpitch</td>
<td>32.42</td>
<td>3.19</td>
<td>.03</td>
<td>.026</td>
<td>Linear 13.47</td>
<td>3.40</td>
<td>.68</td>
</tr>
<tr>
<td>melint</td>
<td>31.57</td>
<td>3.02</td>
<td>.03</td>
<td>.033</td>
<td>Linear 18.99</td>
<td>3.43</td>
<td>.62</td>
</tr>
<tr>
<td>csd</td>
<td>29.95</td>
<td>3.77</td>
<td>.04</td>
<td>.013</td>
<td>Linear 16.38</td>
<td>3.85</td>
<td>.69</td>
</tr>
<tr>
<td>selection</td>
<td>29.80</td>
<td>3.77</td>
<td>.04</td>
<td>.013</td>
<td>Linear 16.38</td>
<td>3.85</td>
<td>.69</td>
</tr>
<tr>
<td>Cello</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>cpitch</td>
<td>31.18</td>
<td>8.66</td>
<td>.11</td>
<td>&lt;.001</td>
<td>Quadratic 25.39</td>
<td>4.38</td>
<td>.66</td>
</tr>
<tr>
<td>melint</td>
<td>30.72</td>
<td>6.81</td>
<td>.09</td>
<td>&lt;.001</td>
<td>Quadratic 14.04</td>
<td>4.11</td>
<td>.74</td>
</tr>
<tr>
<td>csd</td>
<td>31.25</td>
<td>13.99</td>
<td>.18</td>
<td>&lt;.001</td>
<td>Linear 14.83</td>
<td>4.09</td>
<td>.73</td>
</tr>
<tr>
<td>selection</td>
<td>30.66</td>
<td>14.99</td>
<td>.19</td>
<td>&lt;.001</td>
<td>Linear 13.41</td>
<td>3.83</td>
<td>.72</td>
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<td>Chord events</td>
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<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>vintcc</td>
<td>29.94</td>
<td>6.68</td>
<td>.08</td>
<td>&lt;.001</td>
<td>Linear 16.96</td>
<td>3.56</td>
<td>.65</td>
</tr>
<tr>
<td>csd</td>
<td>31.90</td>
<td>7.02</td>
<td>.09</td>
<td>&lt;.001</td>
<td>Linear 27.04</td>
<td>4.14</td>
<td>.62</td>
</tr>
<tr>
<td>composite</td>
<td>30.91</td>
<td>7.21</td>
<td>.09</td>
<td>&lt;.001</td>
<td>Linear 19.23</td>
<td>4.81</td>
<td>.74</td>
</tr>
</tbody>
</table>

Note: NS = non-significant. Planned comparisons corrected with Bonferroni adjustment.

6.2.3. Discussion

The mean IC estimates from IDyOM provide strong evidence in support of the Prospective Schemas model of cadential strength. Polynomial contrasts revealed significant positive linear trends for the viewpoints vintcc, csdc, composite, csdVc, and selectionVc, as well as significant positive quadratic trends for cpitchVc, melintVc, and all of the viewpoints for the first violin. Furthermore, the claim that the genuine cadence categories elicit the strongest and most specific schematic expectations appears to be well supported by the experimental results from the second planned comparison, which revealed that the terminal events from the genuine cadence categories produced the lowest IC estimates on average for the viewpoint models from the first violin and across the entire texture, whereas the cadential deviations generally received the highest IC estimates on average.

Takentogether, the reported findings support the role for expectancy in models of cadential strength, with the most complete or closed cadences also serving as the most expected. What is more, the results obtained here replicate the pattern of results reported by Sears, Caplin, and McAdams (2014). In that study, participants indicated how complete they found the end of each of a series...
of cadential excerpts from Mozart’s keyboard sonatas. The genuine cadence categories and the cadential deviations received the highest and lowest completion ratings, respectively, which in light of the present findings suggests that the perceived strength of the cadential ending corresponds with the strength of the schematic expectations it generates in prospect. But recall that the perception of closure also depends on the cessation of expectations following the terminal events of the cadence. That is, the strength of the potential boundary between two sequential events results in part from the increase in information content (or decrease in probability) from the first to the second event (i.e. the last event of one group to the first event of the following group). The preceding analyses examined terminal events from cadential and non-cadential contexts in isolation, so Experiment 3 considers the role played by schematic expectations in boundary perception and event segmentation by examining the time course of IC estimates surrounding the terminal events of the cadence.

6.3. Experiment 3

Experiment 3 examines two claims about the relationship between expectancy and boundary perception: (1) that the terminal event of a group is the most expected (i.e. predictable) event in the surrounding sequence; and (2) that the next event in the sequence is comparatively unexpected (i.e. unpredictable). Again, the hypothesis here is that unexpected events engender prediction errors that lead the perceptual system to segment the event stream into discrete chunks (Kurby & Zacks, 2008). The terminal events from the PAC, IAC and HC categories should be highly predictable, and prediction errors for the comparatively unpredictable events that follow should force listeners to segment the preceding cadential material. For the cadential deviations, however, prediction errors should occur at, rather than following, the terminal events of the cadence.

6.3.1. Analysis

In addition to the between-groups factor of cadence category, Experiment 3 includes a between-groups factor of time that consists of three levels: \(e_t\), which represents the terminal event of the group, and \(e_{t-1}\) and \(e_{t+1}\), which represent the immediately surrounding events. With more complex designs like this one, the number of significance tests can become prohibitively large, so we have restricted the investigation to the four viewpoints that serve as reasonable approximations of the two-voice framework characterising the classical cadence: \(\text{selection}_{vl1}\) and \(\text{selection}_{vc}\) to represent the soprano and bass, respectively, and \(\text{vintcc}\) and \(\text{csdc}\) to each represent the entire texture. Experiment 3 analyses these viewpoints using a 5 × 3 two-way ANOVA with between-groups factors of cadence category (PAC, IAC, HC, DC, and EV), and time (\(e_{t-1}, e_t, e_{t+1}\)).

By moving from one to two between-groups factors, the number of omnibus statistics and planned comparisons necessarily increases, and since Levene’s test also revealed heteroscedastic groups for all four of the 5 × 3 viewpoint ANOVAs, the risk of committing a Type I error is considerably greater here than in the previous experiments. In this case, the two hypotheses mentioned above concern the interaction between cadence category and time: namely, whether the IC estimates for each cadence category increase or decrease significantly from one event to the next. Thus, the following analysis ignores the main effects and concentrates only on the interaction term of the two-way ANOVA. If the interaction is significant, we report simple main effects, which represent one-way ANOVAs with time as a factor for each level of cadence category. Finally, to examine the potential differences in the IC estimates for the levels of time for each cadence category, each simple main effect included two planned comparisons with Bonferroni correction that do not assume equal variances: (1) whether the IC estimate for \(e_t\) is lower on average than the surrounding events, \(e_{t-1}\) and \(e_{t+1}\) (\(e_t\ vs. Surrounding\)); and (2) whether the IC
estimate for $e_{t+1}$ is higher on average than the estimate for $e_t$ ($e_t$ vs. $e_{t+1}$).

**6.3.2. Results**

Figure 6 displays line plots of the mean IC estimates for the note events over time in the first violin (top) and cello (bottom) for each cadence category using the viewpoint selection, which represents melint and the linked viewpoint csd@cpitch. The statistical analysis pertains to event numbers $-1, 0$ (or Terminus), and 1. Whiskers represent $\pm 1$ standard error.

For the PAC, IAC, HC, and DC categories, the mean IC estimates increased significantly from $e_t$ to $e_{t+1}$, thereby supporting the view that the strength of the perceptual boundary depends on the increase in information content following the terminal event of the cadence. And yet since the EV category replaces the expected terminal event in the melody with material that clearly initiates the subsequent process—often by leaping up to an unexpected scale degree like $\hat{5}$—one might therefore predict that a significant increase in information content should occur at (and not following) the expected terminal event of the group. This is exactly what we observe, with the expected terminal events from the EV category receiving the highest mean IC estimate in the sequence (see Table 7). Thus, the pattern of results from selection_{all} is entirely consistent with the two main hypotheses: (1) the terminal event of a group is the most predictable event in the sequence, and (2) the next event is comparatively unpredictable. Here, the mean IC estimates for the first violin increased significantly following the predicted boundary for every cadence category in the collection.

For the cello, a two-way ANOVA of the mean IC estimates revealed a significant interaction between cadence category and time, $F(8,717) = 13.02, p < .001, \text{est. } \omega^2 = .12$. Excepting IAC, the mean IC estimates also revealed simple main effects for every level of cadence category. As expected, the terminal event in the cello received lower IC estimates on average than the immediately surrounding events for the HC category, but the trend was reversed for the PAC, DC and EV categories, and the trend for the IAC category was not significant.

For the HC category at least, the terminal event was also the most predictable event in the sequence. Furthermore, the significant increase in information content in the cello at the expected terminal event in the DC and EV categories is consistent with the behaviour of cadential deviations. For the former category, the bass typically resolves deceptively to scale degrees like $\hat{6}$, thereby violating expectations for $\hat{1}$, whereas the latter category evades the expected resolution by leaping to other scale degrees to support harmonies like $I^6$. The significant increase in information content for the terminal event of the PAC category is somewhat more surprising, however. Recall from Experiment 2 that the mean IC estimates for the terminal events from each cadence category in the cello demonstrated a positive quadratic trend, with the HC category receiving the lowest IC estimates (see Figure 4). In that case, we suggested that small melodic intervals appear more abundantly in the corpus than large intervals, resulting in higher IC estimates for categories featuring large leaps (PAC, IAC and EV). From this point of view, it seems reasonable that the mean IC estimates for the cello would increase at $e_t$ for categories featuring
Table 7. Analysis of variance and planned comparisons predicting the information content estimates from selection\_vl, selection\_vc, and vintcc over time for each cadence category.

<table>
<thead>
<tr>
<th>Viewpoint</th>
<th>Omnibus</th>
<th>Comparisons</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>df</td>
<td>Welch F</td>
</tr>
<tr>
<td>PAC</td>
<td>227.67</td>
<td>42.14</td>
</tr>
<tr>
<td>IAC</td>
<td>14.20</td>
<td>3.38</td>
</tr>
<tr>
<td>HC</td>
<td>161.48</td>
<td>15.57</td>
</tr>
<tr>
<td>DC</td>
<td>35.50</td>
<td>8.93</td>
</tr>
<tr>
<td>EV</td>
<td>19.87</td>
<td>8.29</td>
</tr>
</tbody>
</table>

| Note events | df | Welch F | est. $\omega^2$ | p | $e_t$ vs. Surrounding | $e_t$ vs. $e_{t+1}$ |
| selection\_vl | 236.76 | 67.63 | .35 | < .001 | 298.45 | -9.88 | .50 | < .001 | 223.50 | 11.64 | .61 | < .001 |
| IAC       | 14.95 | 3.89 | .02 | NS | 18.48 | -2.79 | .54 | .024 | 12.53 | 2.78 | .54 | .032 |
| HC        | 162.48 | 32.34 | .20 | < .001 | 209.41 | -6.92 | .43 | < .001 | 160.95 | 8.02 | .53 | < .001 |
| DC        | 35.86 | 2.84 | .01 | NS | 36.92 | -2.10 | .33 | .085 | 35.62 | 2.41 | .55 | .043 |
| EV        | 18.67 | 5.22 | .03 | NS | 14.87 | 2.54 | .55 | .043 | 19.23 | -1.58 | .34 | NS |

| Selection\_vc | df | Welch F | est. $\omega^2$ | p | $e_t$ vs. Surrounding | $e_t$ vs. $e_{t+1}$ |
| PAC       | 115.27 | 42.14 | .25 | < .001 | 322.14 | 3.18 | .17 | .003 | 180.58 | 1.65 | .12 | NS |
| IAC       | 14.20 | 3.38 | .02 | NS | 21.98 | 1.98 | .39 | NS | 10.57 | .71 | .21 | NS |
| HC        | 161.48 | 15.57 | .11 | < .001 | 213.66 | 5.44 | .35 | < .001 | 151.11 | 3.76 | .29 | < .001 |
| DC        | 35.50 | 8.93 | .06 | .004 | 43.02 | 2.98 | .41 | .010 | 33.15 | 0.97 | .17 | NS |
| EV        | 19.87 | 8.29 | .06 | .012 | 17.49 | 4.06 | .70 | .002 | 19.22 | -3.19 | .59 | .009 |

Chord events

| vintcc | df | Welch F | est. $\omega^2$ | p | $e_t$ vs. Surrounding | $e_t$ vs. $e_{t+1}$ |
| PAC       | 235.55 | 9.74 | .07 | < .001 | 313.01 | -3.63 | .20 | .001 | 220.21 | 4.42 | .29 | < .001 |
| IAC       | 15.21 | 6.48 | .04 | .046 | 22.58 | -3.49 | .59 | .004 | 13.71 | 2.09 | .49 | NS |
| HC        | 161.39 | 8.26 | .06 | .002 | 216.80 | -4.07 | .27 | < .001 | 157.62 | 3.25 | .25 | .003 |
| DC        | 34.73 | 2.05 | .01 | NS | 38.02 | 1.14 | .18 | NS | 34.51 | 0.05 | .01 | NS |
| EV        | 19.91 | 0.18 | =0 | NS | 18.50 | 0.25 | .06 | NS | 19.98 | 0.04 | .01 | NS |

Note: NS = non-significant. Planned comparisons corrected with Bonferroni adjustment.

large leaps or unexpected scale-degree continuations, as is the case with the PAC, IAC, DC and EV categories.

Given this pattern of results for the cello, it should also come as little surprise that HC was the only category to demonstrate a significant increase in information content following the terminal event of the cadence. To be sure, the IC estimates for the cello did not significantly increase at $e_{t+1}$ for the PAC and IAC categories, thereby undermining the hypothesis that for the genuine cadence categories at least, the perceived boundary follows the terminal events of the cadence. When the results from the first violin and the cello are considered together, HC was also the only category for which the IC estimates from selection\_vl and selection\_vc decreased at $e_t$ and then increased at $e_{t+1}$. If the PAC and IAC categories also generate strong and specific melodic and harmonic expectations for the terminal events of the cadence, the viewpoint models representing both voices of the two-voice framework should demonstrate congruent behaviour.

Figure 7 displays line plots of the mean IC estimates for vintcc (top) and csdc (bottom) over time for each level of cadence category. Two-way ANOVAs of the mean IC estimates revealed a significant interaction between cadence category and time for both viewpoint models (vintcc, $F(8,719) = 3.13$, $p = .002$, est. $\omega^2 = .03$; csdc, $F(8,704) = 2.99$, $p = .003$, est. $\omega^2 = .03$). Simple main effects and planned comparisons were not significant for csdc, however, so it will not be reported here. For vintcc, the mean IC estimates revealed simple main effects for the genuine cadence categories, but not for the cadential deviations. As expected, the terminal chord event received lower IC estimates on average compared to the surrounding events for the genuine cadence categories. Although the trend was reversed for the cadential deviations, with the mean IC estimates increasing from $e_{t-1}$ to $e_t$, the difference was not significant for either category. Finally, the mean IC estimates increased significantly from $e_t$ to $e_{t+1}$ for PAC and HC, but this trend was marginal for IAC.

6.3.3. Discussion

The viewpoint model for vintcc demonstrated a similar trend to that found in selection\_vl for the genuine cadence categories, with the mean IC estimates decreasing from $e_{t-1}$ to $e_t$, and then increasing from $e_t$ to $e_{t+1}$. These two viewpoint models also displayed congruent behaviour for the EV category, with both models increasing from $e_{t-1}$ to $e_t$, suggesting that the perceptual boundary precedes (rather than follows) the expected terminal event in evaded cadences. For the DC category, parametric noncongruence obtained, with the mean IC estimates at $e_t$ decreasing in selection\_vl but increasing in vintcc. Thus, across the levels of cadence category and time, the selection\_vl and vintcc viewpoint models supported our initial hypotheses: (1) the terminal event of a group is the most expected (i.e. predictable)...
the terminal events from half-cadential contexts were composite and represent ± effects were limited to the chord models (vintcc, csdc, and composite) and the csd viewpoint model, but the terminal events from half-cadential contexts were still more predictable than those from non-cadential contexts. Experiment 2 provided strong evidence in support of the Prospective Schemas model of cadential strength (PAC→IAC→HC→DC→EV), with the genuine cadence categories (PAC, IAC, HC) and cadential deviations (DC, EV) in Caplin’s typology eliciting the lowest and highest IC estimates on average, respectively. Finally, the results from Experiment 3 indicated that unexpected events—like those directly following the terminal note and chord events from genuine cadences—engender prediction errors that presumably lead the perceptual system to segment the event stream immediately following the cadential process.

Taken together, the reported findings support the role of expectancy in models of cadential closure, with the most complete or closed cadences also serving as the most expected or probable. Nevertheless, future studies will need to address a number of limitations in the current investigation. First, the rather meager sample size for three of the five cadence categories in the collection—as well as the corpus more generally—casts some doubt upon the generalisability of the reported findings. That the estimates from IDyOM correspond so well with theoretical predictions suggests that these findings may be robust to issues of sample size, but future studies should look to expand the collection considerably, as well as to consider how the relationship between expectancy and cadential closure varies for other genres and style periods.

Second, we selected individual viewpoints if existing theoretical or experimental evidence justified their inclusion, such as melint and csd in melodic contexts (Dowling, 1981; Krumhansl, 1990), and vintcc and csdc in harmonic contexts (Gjerdingen, 2007). Yet in a few instances, cpitch—which was only included among the melodic viewpoints to serve as a baseline for model comparison—produced similar results (see Experiment 2). One reason for this finding is that many of the viewpoints characterising melodic organisation in Haydn’s string quartets systematically covary such that statistical regularities governing the more cognitively plausible viewpoints (e.g. melint and csd) also appear in the less plausible ones (cpitch), albeit more weakly. In a melody composed in the key of C-major, for example, B♭ presumably functions as the leading tone, not because the twelve-tone chromatic universe regularly features this two-note sequence regardless of the particular tonal context, but because C♮ typically follows B♭ in the key of C-major, forming one of the many statistical associations characterising the tonal system. Nevertheless, the tendency for small melodic intervals and the prevalence of certain keys in tonal music—wherein B♭ is more likely to progress to C♮ than to, say, A♭—ensures that IDyOM will learn statistical regularities in basic view-

Figure 7. Time course of the mean IC estimated for the events surrounding the terminal chord event for vintcc (top) and csdc (bottom) for each cadence category. The statistical analysis pertains to event numbers −1, 0 (or Terminus), and 1. Whiskers represent ±1 standard error.

7. Conclusions

This study examined three claims about the relationship between expectancy and cadential closure: (1) terminal events from cadential contexts are more predictable than those from non-cadential contexts; (2) models of cadential strength advanced in cadence typologies like the one employed here reflect the formation, violation, and fulfilment of schematic expectations; and (3) a significant decrease in predictability follows the terminal note and chord events of the cadential process. To that end, we created a corpus of Haydn string quartets to serve as a proxy for the musical experiences of listeners situated in the classical style, selected a number of viewpoints to represent suitable (i.e. cognitively plausible) representations of the musical surface, and then employed IDyOM—an n-gram model that predicts the next note or chord event in a musical stimulus through unsupervised learning of sequential structure—to simulate the formation of schematic expectations during music listening.

The findings from Experiment 1 indicate that the terminal note and chord events from perfect authentic cadences are more predictable than (1) non-cadential events featuring tonic harmony in root position and supporting any scale degree in the soprano, and (2) non-cadential events featuring any other harmony and any other scale degree in the soprano. For half cadences, significant effects were limited to the chord models (vintcc, csdc, and composite) and the csd viewpoint model, but the terminal events from half-cadential contexts were
points like \textit{cpitch} that are correlated to those found in other melodic viewpoints like \textit{melint} or \textit{csd}.

What is more, rather than assume that listeners expect specific intervals in a melodic sequence, as is IDyOM’s approach using \textit{melint}, existing models of melodic expectation typically theorise that listeners expect smaller melodic intervals regardless of the preceding context, a principle known as \textit{pitch proximity} (e.g. Cuddy & Lunney, 1995; Margulis, 2005; Narmour, 1990; Schellenberg, 1997). Yet in this study, we only assume that listeners form expectations on the basis of statistical regularities among melodic intervals in a sequence. Vos and Troost (1989) have demonstrated, for example, that small intervals are far more common than large intervals in Western tonal music, so it should not be surprising that IDyOM produces higher probability estimates for smaller intervals, just as do proximity-based models. The difference in these two approaches is thus theoretical, rather than empirical, in that IDyOM bases its predictions on a theory of implicit statistical learning, whereas proximity-based models also sometimes base their assumptions on other (sensory or psychoacoustic) mechanisms. It is certainly possible that these mechanisms influence the preference for smaller over larger intervals in Western tonal music—or indeed, the formation of expectations during music listening more generally—but we do not examine this assumption here.

Perhaps more importantly, the cross entropy estimates for the melodic models in this study indicate that IDyOM was more certain about its predictions for more cognitively plausible viewpoints like \textit{melint} and \textit{csd} than for less plausible ones like \textit{cpitch}, thereby reinforcing the view that representations of the musical surface are ‘cognitively plausible’ to the degree that they minimise prediction errors for future events (Pearce & Wiggins, 2012). Indeed, if prediction is the ‘primary function’ of the brain (Hawkins & Blakeslee, 2004, p. 89), and listeners learn to compress information during processing by only retaining representations of the musical surface that minimise uncertainty (Pearce & Wiggins, 2012), it therefore seems reasonable to include \textit{cpitch} and \textit{melint} among a potentially large number of candidate viewpoints in the initial model configuration and allow IDyOM to select the viewpoint (or combination of viewpoints) that minimises uncertainty empirically (i.e. in an unsupervised manner). Furthermore, in this case IDyOM benefited from human annotations of tonal information in \textit{csd}, but future studies could employ viewpoints like the General Chord Type (GCT) representation (Cambouropoulos, 2015), which automatically produces Roman numeral-like encodings of complex polyphonic corpora.

Third, IDyOM’s modelling architecture could be further improved to more closely resemble the mechanisms by which listeners form expectations for future events. A number of studies in the language modelling literature have demonstrated the utility of non-contiguous \textit{n}-grams for the discovery and classification of recurrent patterns (i.e. collocations) (Guthrie, Allison, Liu, Guthrie, & Wilks, 2006; Huang, Beeferman, & Huang, 1999; Simons, Ney, & Martin, 1997), but the present investigation was limited to contiguous \textit{n}-grams. Creel, Newport, and Aslin (2004) have shown, for example, that listeners can learn non-contiguous statistical regularities in melodic sequences if the intervening events are segregated in terms of pitch height or timbre. What is more, Gjerdingen (2014) has suggested that for stimuli demonstrating hierarchical structure, non-contiguous events often serve as focal points in the syntax. This problem is particularly acute for corpus studies of tonal harmony, where the musical surface contains considerable repetition, and many of the vertical sonorities from the notated score do not represent triads or seventh chords, thereby obscuring the most recurrent patterns. IDyOM is presently capable of including non-contiguous \textit{n}-grams using \textit{threaded} viewpoints, which sample events from a base viewpoint like \textit{cpitch} according to some test viewpoint that represents positions in the sequence, such as metric downbeats or phrase boundaries. Pearce (2005) has shown that these viewpoints improve model performance in melodic prediction tasks, so it is possible that they may also improve model predictions for the terminal events from cadential contexts.

Finally, the present approach depended entirely on simulation. If the brain is a ‘prediction machine’ that generates expectations about future events by forming associations between co-occurring attributes within the external environment, as some have suggested (Bar, 2007; Clark, 2013), then behavioural and neural manifestations of expectancy formation, violation, and fulfilment should correspond in some way with the model simulations reported in this study. In this case, the model estimates generated by IDyOM support the view that cadences and other recurrent closing patterns serve as the most predictable, probabilistic, specifically envisaged formulae in all of tonal music (Huron, 2006; Meyer, 1956). To demonstrate further that the schematic expectations formed by listeners for cadences and other recurrent temporal patterns amount to these sorts of probabilistic inferences requires an entirely different approach, one in which the listener, rather than the music, represents the primary object of study.
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